

Fuzzy Image Segmentation using Membership Connectedness

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Abstract: Fuzzy connectedness and fuzzy clustering are two well-known techniques for fuzzy image segmentation. The former considers the relation of pixels in the spatial space, but does not inherently utilize their feature information. On the other hand, the latter does not consider the spatial relations among pixels. In this paper, a new segmentation algorithm is proposed in which these methods are combined via a notion called membership connectedness. In this algorithm, two kinds of local spatial attractions are considered in the functional form of membership connectedness and the required seeds can be selected automatically. The performance of the proposed method is evaluated using a developed synthetic image dataset and both simulated and real brain *magnetic resonance image* (MRI) datasets. The evaluation demonstrates the strength of the proposed algorithm in segmentation of noisy images which plays an important role especially in medical image applications.

Keywords: Membership connectedness, fuzzy connectedness, fuzzy clustering, magnetic resonance image, image segmentation.

1. Introduction

Image segmentation is one of the most challenging and critical problems in image analysis. Segmentation processes aim at partitioning the image plane into “meaningful” regions (where meaningful typically refers to separation of image regions into different semantic objects). As image segmentation is the core of many image analysis problems, any improvement in segmentation methods can lead to important impacts on many image processing and computer vision applications.

Challenges in image segmentation has encouraged researchers to develop fuzzy segmentation algorithms by considering image regions as fuzzy subsets (fuzzy objects), where an image pixel may be partially classified into multiple potential classes and the boundaries between intensities of different objects can be well defined. Here, the theory of fuzzy sets [1] is adopted to effectively model the fuzziness of image pixels which might be caused by inherent object material heterogeneity and imaging device artifacts (*e.g.*, blurring, imposed noise, and background variation).

There are several image segmentation methods based on fuzzy concept reported in the literature [2-4] among which fuzzy connectedness [5] and fuzzy clustering [4] are two well-known techniques for this purpose. Moreover, fuzzy rule-based methods [2, 6-8], fuzzy thresholding [3, 9-11], fuzzy markov random

field [12-14], and fuzzy region growing [15, 16] are also reported for region-based fuzzy segmentation. Fuzzy connectedness is a fuzzy topological property [17] and defines how the image pixels are spatially related in spite of their gradation of intensities [18]. The classical definition of fuzzy connectedness was given by *Rosenfeld* in [19]. A modification to this traditional concept, called *intensity connectedness*, was proposed in [20]. Fuzzy connectedness for image segmentation was developed by *Udupa* and *Samarasekera* in [5] by notion of a fuzzy object in an N -dimensional space. In defining fuzzy objects in a given image, the strength of connectedness between every two pairs of image pixels is considered. This is determined by considering all possible connecting paths between the pair. In spite of its high combinatorial complexity, theoretical advances in fuzzy connectedness have made it possible to delineate objects via a dynamic programming close to interactive speeds on modern PCs [5].

The abovementioned works apply fuzzy connectedness directly on the given image. But, direct utilization does not inherently consider feature space information as used in fuzzy clustering techniques. Consequently, the affinity function is defined. This definition requires dynamic computation of the weights and automatic computation of a threshold which requires an exhaustive search cost. This issue is very critical in applications such as analysis of *magnetic resonance* (MR) images, where optimal combination of affinity component weights varies for each slice and each subject [21] in spite of data being acquired from the same MR scanner with identical protocol. As such, in [21] a method based on dynamic weights is introduced. But, these methods depend on manual selection of object seeds (which is time consuming and may cause errors especially in multi-component objects). As such, a method for automatic seed selection using fuzzy clustering is introduced in [22], but it also applies the fuzzy connectedness directly on the given image.

On the other hand, feature clustering that uses fuzzy clustering techniques, does not take into account any spatial dependency among image pixels and consequently it is sensitive to noise. As the noise removal may eliminate some inherent image information, some methods are recently proposed for integration of spatial information in fuzzy clustering for segmentation applications [23-27].

Considering the abovementioned problems, in this paper we have proposed a new algorithm to combine fuzzy connectedness and fuzzy clustering methods for image segmentation purposes. The desired goal is using both spatial and feature space features in image segmentation. These methods might be integrated tightly in a single algorithm or combined (similar to a post processing approach). As these methods utilize the information of dissimilar spaces (feature or spatial) we have adopted the second possibility in this paper. The proposed algorithm is based on construction of fuzzy connectedness relation in membership images, called *membership connectedness*. Two kinds of local spatial attractions are considered in the proposed functional form of membership connectedness relation.

The construction of membership connectedness requires an initial reference pixel (seed) in the object. As

the manual selection of object seeds in multi-component and complicated objects (such as brain tissues) is very time consuming and may cause error, an automatic method for seed selection is also described.

As the seed set for fuzzy object construction can be selected automatically, if the number of objects in the image is known, the proposed algorithm can be applied completely in an unsupervised manner. Moreover, its advantages include a straightforward utilization for color and multi-spectral image segmentation, multi-object segmentation, and multi-seed utilization abilities. Besides, it does not assume any specific characteristic for the adopted fuzzy segmentation method.

The performance of the proposed algorithm is evaluated using a developed synthetic image dataset which contains 720 images, phantom multi-spectral MR images from *brainweb* data set [28], and *IBSR* dataset of real brain MRI [29].

This paper proposes an application domain-independent segmentation algorithm and evaluates its performance on brain tissue of MR images; as this application requires accurate and robust segmentation results in many quantitative studies in medical image analysis. Different characteristics of the proposed segmentation algorithm are advantageous for this application. In fact, since MR scans are often confounded by magnetic field inhomogeneities and partial volume effects (one pixel may be composed of multiple tissue types), modeling of tissues by fuzzy objects and applying fuzzy segmentation are useful in MR image analysis. In addition to the use of fuzzy connectedness idea (which has been successfully applied in medical image segmentation [18, 21]), the proposed algorithm is not based on affinity function and thus the dynamic computation of its optimal parameters for each slice and each subject in MR image analysis is not required. Moreover, its ability in automatic selection of seed pixels eliminates possible manual selection errors in multi-component and complicated brain tissues (such as peripheral cerebrospinal fluid and multiple sclerosis lesions).

This paper is organized as follows. Section 2 briefly reviews the concept of fuzzy connectedness in image segmentation. Section 3 introduces the proposed membership connectedness notion and segmentation algorithm. Section 4 describes experimental results, and finally Section 5 concludes the paper.

2 Fuzzy Connectedness and Image Segmentation

Fuzzy treatment of geometric and topological concepts can be performed in two distinct manners in image segmentation [18]. The first approach applies a fuzzy image segmentation to obtain a fuzzy subset wherein every pixel has a fuzzy object membership assigned to it and then defines the geometric and topological concepts on this fuzzy subset. The second approach develops these concepts directly on the given image, which implies that these concepts have to be integrated with segmentation process.

Considering the first approach, *Rosenfeld* introduced some early work [19, 30] which was followed by *Dellepiane et al.* [20] in an intensity connectedness-based segmentation method. This approach is adopted

in this work.

Introducing the second approach, *Udupa* and *Samarasekera* [5, 18] proposed an algorithm for object definition and segmentation from background, based on fuzzy connectedness which is a topological construct. Fuzzy connectedness characterizes the way that image pixels are related to each other¹ to form an object.

In the latter algorithm, fuzzy connectedness definition is based on a local fuzzy relation called affinity [18]. The affinity between two image pixels depends on their adjacency as well as their intensity-based features' similarity which captures the local spatial relation of image pixels. The following is a general functional form of membership function (μ_κ) of affinity relation (κ) as proposed in [5].

$$\mu_\kappa(c, d) = \mu_\alpha(c, d) g(\mu_\psi(c, d), \mu_\phi(c, d)) \quad (1)$$

where (c, d) denotes a pair of pixels, μ_α is the adjacency function, and μ_ψ and μ_ϕ represent the fuzzy relation of homogeneity-based and object-feature-based components of affinity, respectively [5]. The homogeneity-based component depends on intensity difference of the pair and the maximum allowed inhomogeneity in the desired object. The object feature-based component depends on the closeness of intensity features of desired pair of pixels to the feature values expected for the desired object. These components can be combined by an appropriate $g(\cdot)$ function.

The global fuzzy connectedness between any two image pixels considers the strength of all possible paths between them; where the strength of a particular path is the weakest affinity between the successive pixel pairs along the path. The fuzzy connectedness relation (K) is defined by the membership function [18]

$$\mu_K(c, d) = \max_{p \in P_{cd}} \left[\min_{1 < i \leq l_p} [\mu_\kappa(c_{i-1}, c_i)] \right] \quad (2)$$

where P_{cd} is the set of all paths (a path is a sequence of nearby elements) connecting c to d , l_p is the length of p , and C_i and C_{i-1} are two successive pixels in p .

The fuzzy object is then extracted by expanding it from the initial seed points based on the mentioned global fuzzy connectedness value. For expansion, the connectedness of each image pixel to a particular object (which is equal to the connectedness of the pixel to the initial seed set of the object), is computed. The connectedness of a pixel to a set of reference pixels is the maximum of connectedness degrees to every pixel of set [18], as defined below for set S and arbitrary pixel c , as

$$f_{Ks}(c) = \max_{s \in S} [\mu_K(s, c)]. \quad (3)$$

Finally, thresholding or applying *relative fuzzy connectedness* [31] will result in a crisp object.

The above discussed algorithm was further extended with introduction of object scale, which allowed the

¹ Called "hanging togetherness" in [18].

size of neighborhood to be changed in different image parts [32], and extended in [33] for vectorial images, and in [34] for multi-object segmentation purposes. Another method, called fuzzy connectedness using dynamic weights, was proposed in [21] to introduce directional sensitivity to the homogeneity-based component to dynamically adjust linear weights in the functional form of fuzzy connectedness.

3 Proposed Method

As discussed in previous sections, fuzzy connectedness influences the segmentation result by spatio-topological consideration of the way that image pixels relate together. This advantage becomes more obvious when one compares it with feature-based segmentation algorithms (*i.e.*, fuzzy clustering), which do not take into account any spatial dependency among image pixels. But, applying fuzzy connectedness directly on a gray-level image requires parameter selection and estimation of object features which often require user interaction (which is time consuming and may cause error especially in multi-component objects). In this section, we describe a new algorithm for applying fuzzy connectedness on membership scene (defined in Subsection 3-1, which is resulted by an arbitrary fuzzy segmentation method) via proposed membership connectedness relation. By this relation, fuzzy connectedness and fuzzy clustering are integrated for image segmentation purposes. These methods may be tightly integrated which result in a single algorithm or may be combined similar to a post processing approach. As these methods utilize the information of dissimilar spaces (feature or spatial) we have adopted the second possibility in this paper.

In this section, we start by briefly reviewing some basis definitions in Subsection 3-1; which are required for formulation of membership connectedness relation in Subsection 3-2. In this Subsection, two kinds of local spatial attractions are considered in the functional form of membership connectedness that results in two different relations. Then, we discuss the main proposed segmentation algorithm in detail about seed selection method and fuzzy object expansion algorithm. Finally, the advantages of the proposed segmentation algorithm are introduced.

3-1 Basic Definitions

In this subsection, a basic set of definitions are presented to provide the preliminaries of the membership connectedness formulation. First, we define the membership scene by following the terminology used in [18] and then briefly describe the *fuzzy C-means* (FCM) clustering method.

Let X be any reference set. A fuzzy subset A of X is a set of ordered pairs $A = \{(x, \mu_A(x)) \mid x \in X\}$, where $\mu_A : x \rightarrow [0, 1]$ is the membership function of A in X (μ is subscripted by the fuzzy subset under consideration). A fuzzy relation ρ in X is a fuzzy subset of $X \times X$ and the pair (X, ρ) is called a fuzzy space when ρ is reflexive and symmetric. If $X = Z^n$ (*i.e.*, the set of n -tuples of integers), ρ is called

adjacency and the pair (Z^n, ρ) is called digital fuzzy space. Fuzzy digital space is a concept that characterizes the underlying digital grid independent of any image related concept. It is desirable that μ_ρ be a nonincreasing function of the distance in Z^n . In a fuzzy digital space, any scalar function $f: C \rightarrow [L, H]$ from a finite subset of C of Z^n to a finite subset $[L, H]$ of the integers defines a scene (C, f) over (Z^n, ρ) . When the scene intensity represents the fuzzy membership value in $[0, 1]$, we call it the membership scene. In image processing field, membership scenes can be obtained by any fuzzy clustering method.

Fuzzy cluster analysis allows data points to have partial memberships to different clusters which is measured as degrees in $[0, 1]$. This yields to the flexibility that data points can belong to more than one cluster. As a well-known method in this field, fuzzy C-means clustering method [35] minimizes the below objective function

$$J(U, V) = \sum_{k=1}^n \sum_{i=1}^c (u_{ik})^m \|x_k - v_i\|$$

subject to

$$u_{ik} \in [0, 1],$$

$$\forall k \sum_{i=1}^c u_{ik} = 1$$

(4)

where $\mathbf{X} = \{\mathbf{x}_1, \mathbf{x}_2, \dots, \mathbf{x}_n\}$ is the given data set, c is the number of clusters. The $c \times n$ matrix $U = (u_{ij})$ is called the fuzzy partition matrix, where u_{ij} denotes the membership degree of a datum x_j to cluster i , v_i is the prototype of the i^{th} cluster and m ($m > 1$) is called the fuzzifier parameter which is usually chosen 2.

Based on the abovementioned fuzzy cluster notion, we are now better prepared to handle the ambiguity of cluster assignments when clusters are unwillingly delineated or overlapped. When we consider the different objects of an image as different clusters and the segmentation process as a clustering problem, the resulted fuzzy clusters correspond to fuzzy objects of the image and u_{ij} denotes the membership degree of pixel x_j to object i .

3-2 Membership Connectedness

In this subsection, two different fuzzy relations are proposed that can be used as a membership connectedness relation in the proposed segmentation algorithm (described in Subsection 3-3).

A. Direct Membership Connectedness Relation

Let $I \in Z^2$ be related to the underlying grid of image and $M = (I, \mu_o)$ be any membership scene corresponding to a desired fuzzy object o resulted by an arbitrary fuzzy segmentation. In order to consider

spatial relations among image pixels, the membership connectedness fuzzy relation m in I is defined as

$$\mu_m(c, d) = \max_{p \in P_{cd}} \left[\min_{1 \leq i \leq l_p} (\mu_o(c_i)) \right] \quad (5)$$

where (c, d) is a pair of pixels, P_{cd} is the set of all paths (a path is a sequence of nearby elements) connecting c to d , l_p is the length of p and c_i is a pixel in the path sequence. In this relation, neighborhood characteristics of pixels are considered. If the membership degree of a noisy pixel c to an object is higher than the true value (the *false positive* (FP) error), it may be corrected using (5) in the described segmentation algorithm defined in Subsection 3-3. In this paper, the defined relation in (5) is called *direct membership connectedness* (direct_MC).

B. Indirect Membership Connectedness Relation

In definition of membership connectedness relation, if the local interaction of adjacent pixels is considered as well as neighborhood characteristics, the membership connectedness m can be defined by

$$\mu_m(c, d) = \max_{p \in P_{cd}} \left[\min_{1 < i \leq l_p} [\mu_\kappa(c_{i-1}, c_i)] \right] \quad (6)$$

where c_i and c_{i-1} are two successive pixels and κ is a local fuzzy relation based on adjacency defined as

$$\mu_\kappa(c, d) = \mu_\alpha(c, d) g(\mu_\psi(c, d), \mu_\phi(c, d)) \quad (7)$$

where μ_α is the adjacency function (the 4-adjacency [36] function is assumed in this paper), and μ_ψ and μ_ϕ represent the fuzzy relation of homogeneity-based and object feature-based components of κ similar to affinity definition in (1). The μ_ψ function depends on the difference of membership degree of the pair and μ_ϕ component depends on the average of membership degree of desired pair of pixels. These components are generally defined by

$$\mu_\psi(c, d) = \sum_{\substack{e \in N_c, f \in N_d \\ c-e-d-f=\text{diff}}} w_{\text{diff}} \times L(\mu_o(e) - \mu_o(f)) \quad (8)$$

$$\mu_\phi(c, d) = \sum_{\substack{e \in N_c, f \in N_d \\ c-e-d-f=\text{diff}}} w_{\text{diff}} \times \frac{1}{2} (G(\mu_o(e)) + G(\mu_o(f))) \quad (9)$$

and combined by the geometric mean function $g(\cdot)$. In above relations, N_c and N_d are the defined neighborhood set for c and d , e and f are corresponding pixels in N_c and N_d , W is weighting function, and L and G are Laplacian and mixture of Gaussian distributions, respectively. In this paper, a simplified version of the above relation which produces nearly the same result is used in order to reduce the execution time, as follows

$$\mu_{\phi}(c, d) = 1 - |\mu_o(c) - \mu_o(d)| \quad (10)$$

$$\mu_{\phi}(c, d) = \frac{1}{2}(\mu_o(c) + \mu_o(d)). \quad (11)$$

The defined relation in (6) is called *indirect membership connectedness* (indirect_MC). Because the interaction of pixels is considered in this relation, a noisy pixel with higher or lower membership degree than the true value (FP and *false negative* (FN) errors, respectively) may be corrected using indirect_MC in the segmentation algorithm described in Subsection 3-3.

3-3 Algorithms

In this section, the main proposed segmentation algorithm is introduced and the two steps of the algorithm called automatic selection of seed pixels and fuzzy object expansion are explained.

A. Main Algorithm

The main steps of the proposed image segmentation algorithm are as follow.

1. Apply an arbitrary fuzzy segmentation algorithm (e.g., FCM clustering) which results in fuzzy objects $\{O_i, i=1 \dots n\}$ (n : number of objects in the image).
2. for each O_i do
 - a. Extract initial seed set (S_i) automatically (or manually), using below described method (part B).
 - b. Calculate function f_i of membership connectedness scene (I, f_i) of O_i , using the membership scene (I, μ_o) of O_i and the initial seed set S_i (by using the below described fuzzy object expansion algorithm (part C) based on direct_MC or indirect_MC relations).
3. Extract Crisp objects by applying the maximum classifier on $\{f_i, i=1 \dots n\}$; which assigns each pixel to the most connected object (as done in *relative fuzzy connectedness* [31]).

In this algorithm, the connectedness to an object in Step 3 means the connectedness to its set of reference pixels (using μ_m instead of μ_k in relation (3)).

B. Automatic Selection of Seed Pixels

As the second part of the proposed algorithm applies a region-based segmentation process, the delineation of an object (Step 2-b of the algorithm) requires some initial seeds for object expansion. These seeds may be provided by manual selection; but it requires user interaction and might cause errors in multi-component and complicated objects. In this subsection, the utilized method for automatic selection of seeds in the proposed algorithm is described.

The required initial seed set (S in the described algorithm) can be selected by thresholding the function of

membership scene of the desired object (μ_o) by

$$S = \{c \mid c \in I, \mu_o(c) \geq \theta\} \quad (12)$$

where I is the underlying grid of image under consideration, and θ is the selected threshold in the range of $[0,1]$. In order to avoid the selection of a noisy pixel as a seed, a directional smoothing filter [37] is applied on the normalized membership image (resulted by considering the membership degree as the pixel intensity) before the thresholding step. For small θ , the spatial space information of the image is not included as feature space information in segmentation algorithm and the obtained result is more similar to the feature clustering result (the first step of the proposed algorithm). In this case, some noisy pixels might be selected as seed points. On the other hand, for large θ , there might be no selected seed in some components of an object and they might be missed. Both cases lead segmentation error. Our conducted experimental results indicated the θ equal to 0.9 is an appropriate value.

C. Fuzzy Object Expansion Algorithm

We have adopted the κ FOEMS algorithm [18] (which is based on dynamic programming) for fuzzy object expansion from initial seeds in the proposed segmentation algorithm. In the following algorithm $f(c) = \max_{s \in S} [\mu_m(s, c)]$ is calculated for all pixels $c \in I$ by using the membership scene (I, μ_o) and the seed set S . In order to apply the above described algorithm based on direct_MC relation, we set $\mu_k(c, d) = \min[\mu_o(c), \mu_o(d)]$ if c and d are neighboring pixels and 0 otherwise. For applying the indirect_MC relation, μ_k is used as (7).

1. Set $f(c)$ to 0, for $c \in I$ except for those pixels $c \in S$ which are set to $\mu_o(c)$.
2. Push all pixels $c \in I$ such that for some $s \in S, \mu_k(s, c) > 0$ to Q .
3. While Q is not empty do
 - a. Remove a pixel c from Q .
 - b. Find $f_{\max} = \max_{d \in I} [\min(f(d), \mu_k(c, d))]$.
 - c. If $f_{\max} > f(c)$ then
 - i. Set $f(c) = f_{\max}$.
 - ii. Push all pixels e such that $\min[f_{\max}, \mu_k(c, e)] > f(e)$ to Q .
 - d. End if
4. End while
5. End

D. Advantages

The proposed membership connectedness-based image segmentation method enjoys the following advantages. As feature space-based segmentation is an appropriate notion for multi-spectral (or multi-parametric) image segmentation processes, utilization of the proposed algorithm for multi-spectral images is a straightforward task. In this algorithm, objects are indicated by more than one seed, which is often more natural and easier than a single seed object identification. It is also necessary for detection of multi-component objects and reduces the execution time. When one uses fuzzy connectedness relation directly for image segmentation, the intensity-based information of an object should be embedded in the affinity function. This information involves distribution of intensity and its inhomogeneities which are provided by selection or estimation of a series of parameters (e.g., in [21] the distributions are assumed to be Gaussian and their parameters are estimated from a 5×5 sample region of object). In the proposed algorithm, which is independent from utilized fuzzy segmentation method, the required information can be provided by an appropriate and available fuzzy segmentation method in the first step.

4 Experimental Results

Image segmentation based on fuzzy connectedness has been successfully applied in medical image segmentation [18, 21]. Following this trend, we evaluated the proposed membership connectedness-based segmentation algorithm on brain MRI segmentation (which is a challenging problem in this field). The properties of utilized brain MR image datasets in this experiment are described in Section 4-1. But, in evaluating segmentation algorithms on medical data, the definition of an absolute ground truth is a main challenge. Consequently, a synthetic image data set is developed and used for more accurate numerical evaluation. Properties and evaluation remarks of both datasets are described in Section 4-1. In this section, in order to have a more precise evaluation, a simulated manual seed selection method is introduced.

In the following experiments, the first step of the proposed algorithm is performed by FCM and is applied on the whole 3D volume of simulated brain dataset. In order to reduce the effect of convergence to local minima of the FCM algorithm, the given results are the average of three different executions of FCM.

Because of utilization of FCM in the first step of our algorithm, the obtained results of the algorithm are first compared with FCM in Subsection 4-2. In this comparison, the ability of the proposed method in improving the performance of the well-known FCM method (especially in noisy image segmentation) is evaluated. Moreover, the results are compared with some recently published MRI segmentation methods (in Subsection 4-3) to show the current status of the MRI segmentation problem and to show the capability of the proposed algorithm in overcoming this challenging problem.

4.1 Dataset and Evaluation Remark

A synthetic image data set was developed to assess the robustness of the proposed method. Each image has 200×200 pixels and its quality can be described by some parameters such as contrast, additive noise (bias), and multiplicative noise (gain). Contrast is the basis for image perception and plays a vital role in defining image quality. Using image intensities, it is defined as $|SA-SB| / (SA+SB)$, where SA and SB denote foreground and background intensities, respectively [21]. We used 5 different degrees of contrast level (similar to [21]) where low values demonstrate objects with small neighboring objects contrasts. Moreover, additive noise (caused by inaccuracies imposed by the nature of scanners in imaging systems) is modeled with 4 varying degrees of zero-mean white Gaussian noise. Finally, considering gradual changes in intensity gain factor, 9 multiplicative noise levels were used in creating the database. Each level is modeled as 4 different gain fields described in [21]. The final database is created using the image model

$$I(x) = g(x) \times f(x) + b(x) \quad (13)$$

where I and f are the observed and image intensity function, respectively, and g and b are the multiplicative and additive noise functions, respectively. As such, the generated database contains $720 = 5 \times 4 \times 9 \times 4$ images.

Moreover, two experiments were performed on both simulated and real brain MRI datasets. The digital brain phantom was provided by Montreal neurologic institute (*Brainweb*) [28]. The “normal” data of *T1-weighted*, *T2-weighted* and *proton density* (PD) images with different noise and intensity inhomogeneities levels with matrix size $181 \times 217 \times 181$ and voxel size 1 mm^3 were used for quantitative evaluation. The real brain MR images and corresponding manually-guided expert segmentation results was provided by the *internet brain segmentation repository* (IBSR)[29]. The 20 normal T1-weighted MR brain data sets in coronal view and their manual segmentations were utilized in our experiments. The in-plane voxel size of these datasets was 1.0 mm and the slice thickness was 3.0 mm.

To evaluate the performance of the proposed segmentation algorithm, its accuracy and efficiency was measured. Regarding the accuracy, the *Dice* similarity coefficient [38], the *Tanimoto* coefficient [39], and the segmentation accuracy were measured between the segmented volume indicated by our algorithm and the ground truth. The *Dice* similarity coefficient measured the ratio between intersection and sum of compared volumes [38]. The *Tanimoto* coefficient indicated the ratio between intersection and union of compared volumes [39] and the segmentation accuracy showed the percentage of correctly classified voxels. These measures ranged from 0 (for no correctly segmented pixel) to 1 (for the totally correct segmentation). To study the behavior of the segmentation algorithm using segmentation accuracy, it is measured on the whole *region of interest* (ROI) which consists of several classes. Moreover, the *true positive volume fraction* (TPVF) and *false positive volume fraction* (FPVF) [33] are also measured. TPVF

measures the ratio between intersection of compare volumes and volume of ground truth. FPVF measures the ratio between the difference of segmented volume and ground truth, and volume of ground truth. Also, regarding the efficiency, the computational time of the proposed algorithm was measured.

The selection of seeds in the following experiments was applied using both automatic (described in Section 3-3) and simulated manual methods. The simulated manual selection was applied in conducted experiments to provide some optimum and error free seeds (to show an obtained segmentation which is not influenced by possible errors of seed selection step (noisy seeds or missed ones) as a reference). It was simulated by selection of seeds from the original (phantom) images as such there were at least one seed in any connected component of the desired object.

4.2 Evaluation and Discussion

In the first experiment, the algorithm was applied on the synthetic image dataset. Fig. 1 shows a typical input image that contains a multi-component object with complicated boundaries and different component sizes. In this figure, a noisy image of the dataset with high amount of additive and multiplicative noise along with the segmentation result of both FCM and the proposed algorithms (direct-MC and indirect-MC) are shown. This figure shows that the proposed algorithm reduces the sensitivity of FCM to noise. Moreover, it shows that the indirect_MC relation outperforms the direct_MC relation. As discussed in Subsection 3-2, the indirect_MC relation has the capability of correcting both FP and FN errors caused by noisy pixels, but the direct_MC relation may only correct FP error. The threshold for selection of reference pixels in these experiments was 0.9.

Fig. 2 shows the results of our algorithm versus different levels of additive noise, gain and contrast, separately. In the depicted diagram, for each factor, the plotted segmentation accuracy is the average resultant accuracy of other factors. As shown in this figure, as the additive noise level (which influences the FCM the most) increases the improvement of the proposed algorithm increases as well. It also shows that in medium contrast levels the improvement is the most and the improvement in different gain levels and different gain types is nearly constant.

In the second experiment, the segmentation of intracranial brain tissues (*white matter* (WM), *gray matter* (GM), and *cerebrospinal fluid* (CSF)) is defined. Assuming 3 clusters for FCM, the algorithm is applied on the whole slices of brain volume (containing all of these three kinds of tissues) and the intracranial brain mask is extracted from the provided phantom. In this experiment, both Brainweb and IBSR data sets were used.

The result of applying the proposed algorithm on different datasets of brainweb with different noise levels is shown in Fig. 3. In this figure, the segmentation accuracy of FCM, direct_MC and indirect_MC algorithms are compared by using automatically selected and optimum seeds. As the segmentation

accuracy is measured on the whole brain volume, it can show the behavior of the compared methods solely. This figure clarifies that the integration of FCM and fuzzy connectedness by proposed MC algorithm, makes FCM robust in segmentation of noisy images, but in the same time utilization of spatial information might often eliminates details of the image. This effect influenced the detection of small isolated CSF regions (these regions can be seen as small white regions in Fig. 4-d) in brain MRI segmentation which might not be connected to any selected seed pixel. These regions can be better detected using only feature space information (as used in FCM). In noiseless images, where FCM performs well in other regions (WM and GM), the utilization of spatial information is not necessary so the superiority of proposed algorithm is not obvious and the discussed effect in CSF segmentation influences the total segmentation accuracy (as shown in low level noise in Fig. 3-a).

It is worth to mention that the proposed segmentation method is a general purpose method that can be applied to a variety of multispectral input images. However, in order to suppress the discussed effect, the proposed algorithm can be specialized for brain MRI segmentation such that MC relation does not apply on CSF membership scenes by skipping Step 2 in main algorithm for CSF region and set $f_i = \mu_o$. This kind of specialization can be applied in any other application in which prior knowledge about existence of such regions is available and they are also detectable after FCM step (In the discussed application the CSF region is detectable because it has the least volume in brain.). Applying this specialization will result in Fig. 3-c. Note that in the indirect_MC case, the membership degrees are changed by the $g(\cdot)$ function in (7) in the generally proposed algorithm. In order to make the unchanged CSF membership degrees comparable with changed ones of WM and GM in Step 3 of the algorithm, $g(\cdot)$ should be selected as $g(x, y) = x \times y$.

In the ideal seed selection case shown in Fig. 3-b, the existence of seeds in any connected component (especially small regions) is guaranteed. Therefore, the discussed problem does not influence the result. This implies that the discussed problem never occurs when error free seeds are available. The discussed specialization for CSF segmentation is applied in evaluations of the brainweb datasets.

Fig. 4 shows the segmentation result of our direct_MC and indirect_MC algorithm using automatic seed selection on a typical slice of high level noise of the brainweb dataset. This figure shows that the resulted regions of both direct_MC and indirect_MC methods are smoother than those of FCM. We would like to mention that brain tissues are complicated and there are long boundaries between them. Therefore, the subjective results of MR image segmentation cannot show the improvement obtained by the proposed algorithm as clear as it can be shown by synthetic images (Fig. 1) or by objective evaluations.

As shown in Fig.4, the most of the remained segmentation error is on the border of regions where cannot be corrected by fuzzy connectedness-based methods. Thus, the results of direct_MC and indirect_MC methods are similar in this application.

For detailed analysis of the algorithm, the TPVF and FPVF are also measured for default dataset of brainweb (which contains 3% of noise and 20% of intensity inhomogeneity). The {TPVF, FPVF} pairs for WM, GM, and CSF is {98.41, 6.53}, {93.53, 3.57}, and {94.20, 3.89}, respectively.

The proposed algorithm was applied on different subjects of IBSR datasets using both automatic and simulated manual seed selection method. In automatic case, there was not any significant improvement on FCM algorithm but using optimum seeds provided by simulated manual selection method there was valuable improvement. Also, the indirect_MC method outperformed the direct_MC method for most of the subjects. Since manual tracing of peripheral CSF is very ill-posed, only the ventricular part of CSF was taken into account in IBSR expert guided segmented images. But, these regions are simply detected by the proposed automatic method. As such, the results obtained by using optimum seeds which did not consider any seed in peripheral CSF regions was much better than those of obtained by using automatically selected seeds. In order to eliminate the remained peripheral CSF regions, a post-processing step was applied by thresholding the CSF membership scene after segmentation algorithms in which the adaptive threshold had been determined using neighborhood pixels of the seeds. After this step, the final segmentation results reached by both direct and indirect MC algorithms were nearly the same. The segmentation results of a typical slice are illustrated in Fig.5. This figure shows that the provided seeds (especially for CSF tissue) and the utilized post-processing method in the proposed algorithm improve the similarity between segmentation result and reference image but the peripheral CSF regions is not removed completely.

In these experiments, we have used Matlab software (except for κFOEMS [18] algorithm that was implemented in C++) on a 1.8-GHz dual core Intel CPU system with 1-GB RAM. The execution time of the proposed algorithm is presented in Table 1 and is compared with FCM runtime. The reported execution time for brainweb is the average runtime on different noise level datasets.

Table 1 Execution time (seconds/image for synthetic and seconds/volume for MR images) of proposed algorithms and FCM.

dataset	FCM	Direct_MC	Indirect_MC
Synthetic	0.48	1.77	2.46
Brainweb	71.87	83.67	98.45
IBSR	5.65	8.95	12.48

4.3 Comparisons

We have also compared the performance of our proposed algorithm to that of other published reports that have recently been applied on brain tissue segmentation on brainweb or IBSR datasets. These include

Ibrahim et al.[40], *Jiménez-Alaniz et al.*[41], *Song et al.*[42], *Solomon et al.* [43] and *Rivera et al.* [44]. It should be mentioned that as the utilized prior information, pre-processing methods and post-processing methods in different reported approaches were not the same, making a fair and meaningful comparison and discussion of segmentation algorithm is not an easy task. Thus, the results given in this section are provided as a reference and some issues should be mentioned before their comparisons. The method in [41] has used prior information in the form of probability maps of voxels and is based on nonparametric density estimation and the mean shift algorithm. In this work the method is applied on part of the brain volume (131 slices). The methods in [40] and [43] are supervised methods and are based on Hidden Markov Models. In [42] a modified probabilistic neural network is utilized for all head MR image segmentations (both brain and background) and the misclassification rate of 3.41% is reported for brainweb dataset. This method is also a supervised method. In [44] an entropy-controlled quadratic markov measure field model is used for segmentation purposes. The algorithms reported in [41, 42] and ours segment all intracranial brain tissues but the other methods do not report the result of CSF segmentation. Tables 2 and 3 list the recent published results on brainweb and IBSR datasets, respectively. The methods compared in Table 2, have been run on images which have 3% of noise and 20% of intensity inhomogeneity and voxel size of 1 mm³. We intended to include the previous fuzzy connectedness-based segmentation methods in this table, but we did not find any published result for the above mentioned dataset. In vectorial fuzzy connectedness segmentation [33] true positive volume fraction is reported for brainweb dataset of voxel size of 3 mm³ (92.6, 95.8, and 94.4 for WM, GM, and CSF, respectively).

Table 2 Accuracy results for a dataset of brainweb [Co.: coefficient].

		direct_MC (optimum seeds)	direct_MC , (automatic seeds)	Ibrahim <i>et al.</i> [40]	Jimenez- Alaniz <i>et al.</i> [41]
Dice Co.	CSF	96.71	96.38	---	---
	WM	96.20	96.04	77.2	
	GM	95.64	95.39	82.8	
Tanimoto Co.	CSF	93.64	93.01	----	87.1
	WM	92.68	92.38		92.4
	GM	91.64	91.18		90.0

As can be seen from this table, the proposed system which does not use any model and training data outperforms the supervised method described in [40] and the method [41] which utilizes prior information of probability maps. It is worth to notice that the achieved results of our proposed algorithm are based on

traditional FCM and thus using improved versions of FCM may lead to better accuracies. Moreover, it was seen that the segmentation error of FCM in the non-noisy images often occurs in the border of regions. Moreover, we were interested in comparing the execution time of our algorithm with that of other methods used for accuracy comparisons. But, unfortunately their execution times were not reported in their papers except for [44] which used a 3-GHz machine.

Table 3: Segmentation accuracy (Tanimoto Coefficient) and efficiency (average execution time per volume) for IBSR dataset.

		direct_MC (optimum seeds)	Ibrahim <i>et al.</i> [40]	Jiménez- Alaniz <i>et al.</i> [41]	Solomon <i>et al.</i> [43]	Rivera <i>et al.</i> [44]
Accuracy	CSF	56.87	--	21.0	--	--
	WM	70.20	66.83	62.8	68.6	74.2
	GM	78.50	77.43	59.4	57.5	81.9
efficiency		8.95 Seconds	--	--	--	3.2 hours

Table 3 shows the results of recent published methods which have been applied on the normal T1-weighted dataset of IBSR. The adopted result of [40] was reported for the case without sudden intensity correction. As can be seen in this table, the proposed algorithm (using optimum seeds selected by simulated manual selection method) outperforms other methods in terms of accuracy except for the method in [44] which is computationally very expensive compared to the proposed method. It also considers the pixels with partial volume of CSF and GM as GM pixels which might eliminate the peripheral CSF parts (which is similarly applied by post-processing stage in our proposed method).

5 Conclusion

A new image segmentation algorithm was proposed in this paper which is based on a combination of fuzzy connectedness and fuzzy clustering approaches via a new definition of fuzzy connectedness in membership images. The evaluation of the proposed method (especially based on the FCM algorithm) shows that the proposed algorithm can reduce the sensitivity of fuzzy segmentation algorithms to noise and decreases the false segmentation results when the noise does not occur on region boundaries. This improvement plays an important role especially in medical image applications. The evaluation of the proposed algorithm on real brain MR images clarifies that the new algorithm can utilize the expert

knowledge in the form of selected seeds and segments the images as desired by the expert. Also, the proposed method can be integrated with any feature-based fuzzy segmentation method adopted for a specific application. Furthermore, the extension of the proposed membership connectedness method using the scale concept may increase the ability of the algorithm in reduction the sensitivity of feature-based segmentation algorithms to noise. Moreover, the integration of the membership connectedness with a hierarchical fuzzy clustering method that does not require the number of objects will result in a fully automatic segmentation algorithm.

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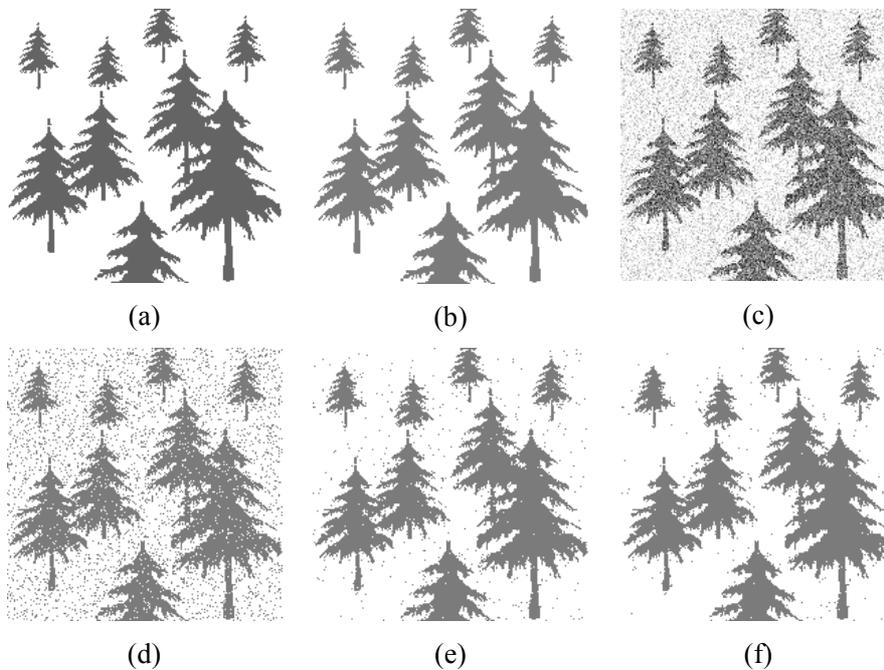
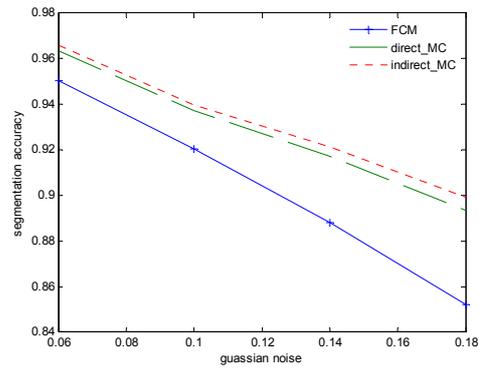
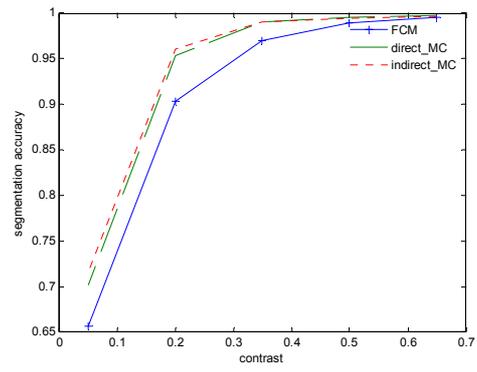


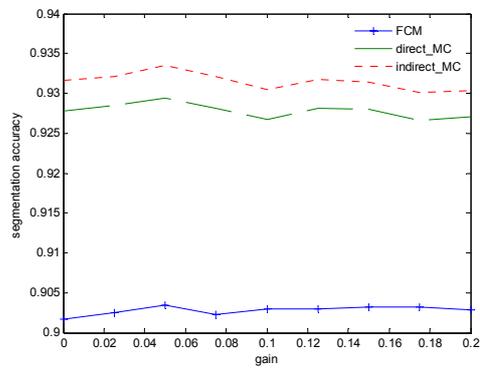
Fig. 1



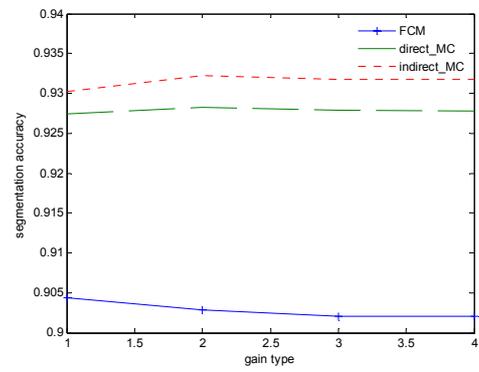
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(b)

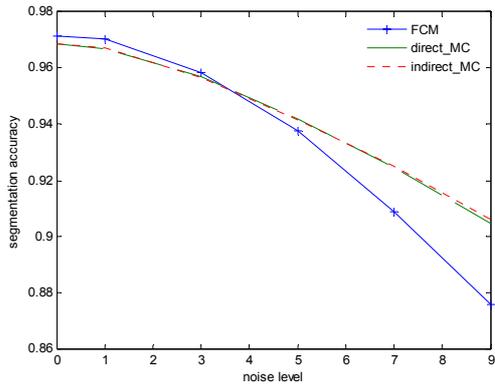


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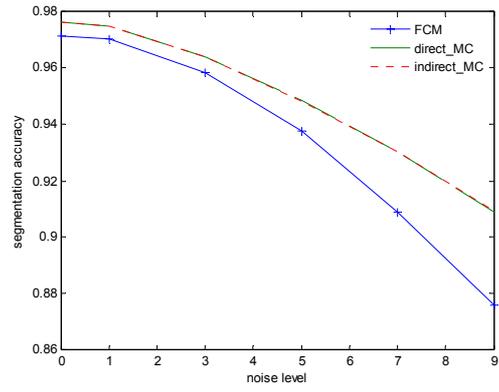


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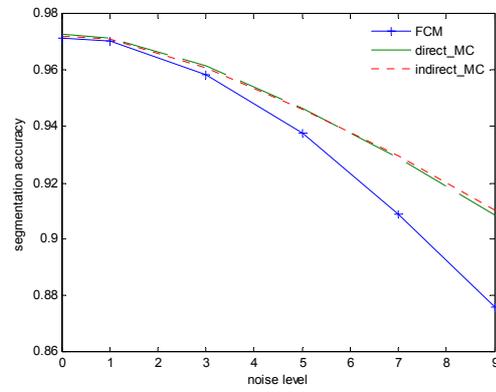
Fig. 2



(a)



(b)



(c)

Fig. 3

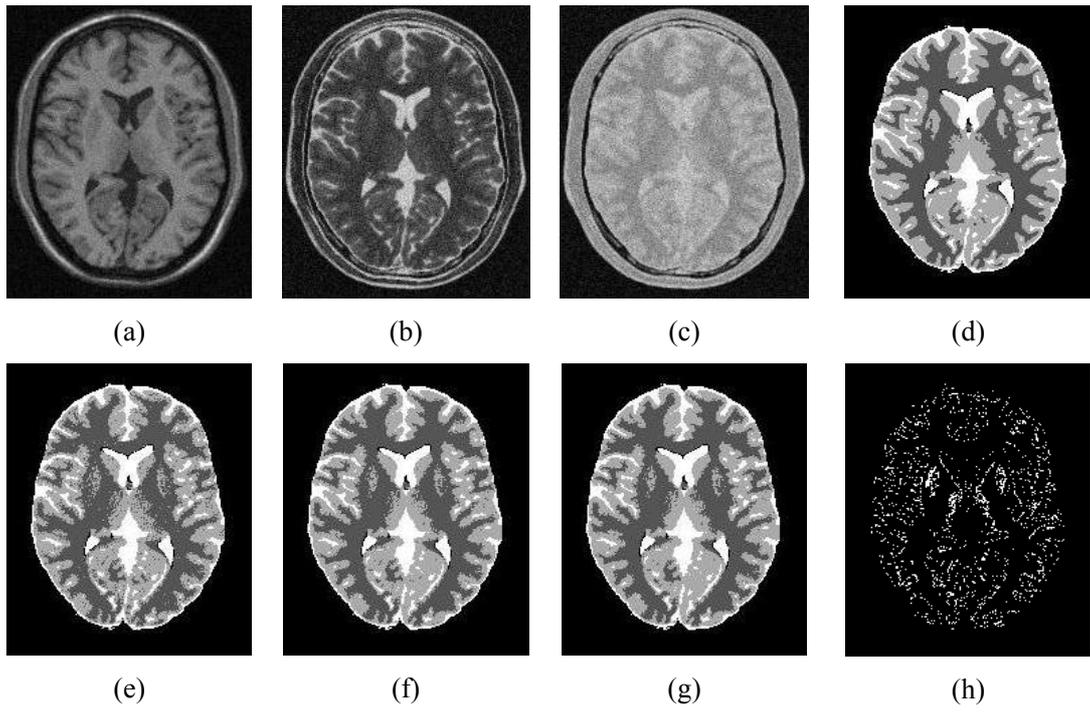


Fig. 4

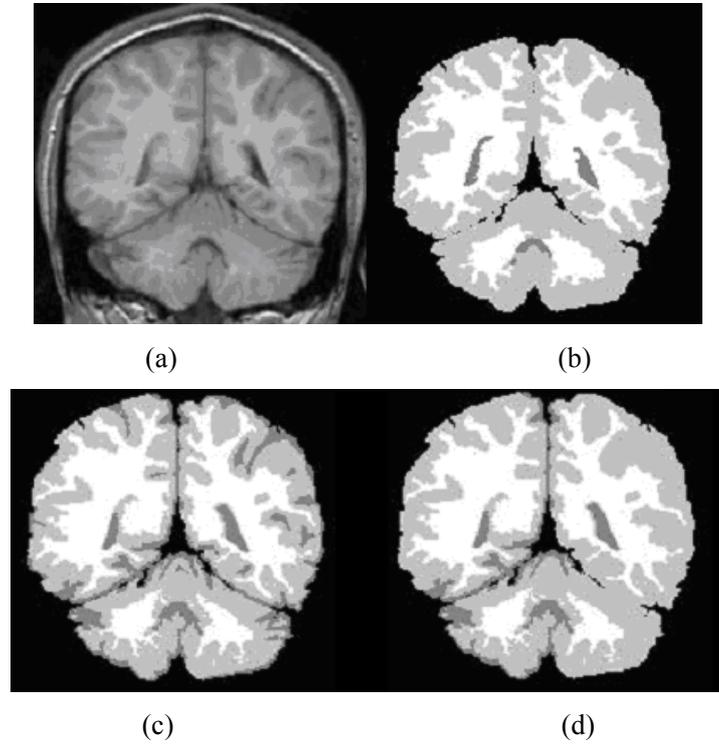


Fig.5